

Breakthrough:

New Solutions to the problem of:

***Instantaneous “Resonant Load”
Parameters Estimation Operating
in “Non-Stationary” Conditions***

Real World → Real Operating Conditions

Two broad categories:

- Stationarity, Deterministic, Periodic....
- Non-Stationarity, Time-Evolving (**T-E**), Transient.....

Extensive field tests conducted by known professionals active in the field of ultrasound conclude that:

many of new ultrasonic applications are highly non-stationary!

There is a need for “Easily Implementable Signal Processing Tools” capable to accurately estimate “Load Parameters” in **“Real-Time”**

The proposed solution is based on:

*Trigonometric properties
of band-limited signals
represented in their
analytical forms*

*It can be shown that “Short-Time” Estimations
are easily obtainable for the following “Time-
Evolving Parameters”:*

*Magnitude of “**Short-Time**” Load
Impedance*

*Argument of “**Short-Time**” Load
Impedance*

“Short-Time” Active/Reactive Power of “Short-Time” Load Impedance”

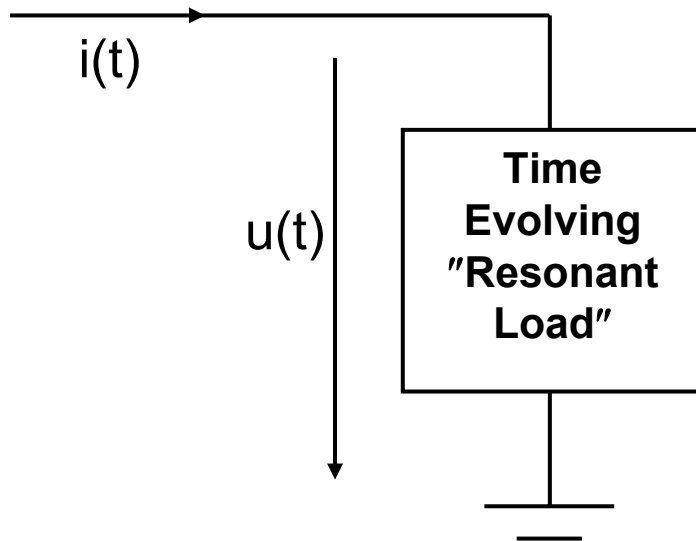
*Instantaneous Frequency of
“Time-Evolving”
Load Voltage or Load Current”*

Basic theoretical analysis

$$i(t) = \hat{I}(t) \cos(2 \cdot \pi \cdot f_o(t) \cdot t + \phi_i(t))$$

$$u(t) = \hat{U}(t) \cos(2 \cdot \pi \cdot f_o(t) \cdot t + \phi_u(t))$$

Basic structure bloc diagram



$\hat{I}(t)$: Instantaneous current envelope

$\phi_i(t)$: Instantaneous current phase

$\hat{U}(t)$: Instantaneous voltage envelope

$\phi_u(t)$: Instantaneous voltage phase

$f_o(t)$: Instantaneous driving signal frequency

Then, $i(t)$ and $u(t)$ can be represented in their respective analytical forms:

$$i(t) \rightarrow i_{\text{analytic}}(t) = i(t) + j \cdot \tilde{i}(t)$$

$$u(t) \rightarrow u_{\text{analytic}}(t) = u(t) + j \cdot \tilde{u}(t)$$

With:

$$\tilde{i}(t) = \hat{I}(t) \cdot \sin(2 \cdot \pi \cdot f_o(t) \cdot t + \phi_i(t))$$

$$\tilde{u}(t) = \hat{U}(t) \cdot \sin(2 \cdot \pi \cdot f_o(t) \cdot t + \phi_u(t))$$

$u(t) \rightarrow$ Hilbert Transformation $\rightarrow \tilde{u}(t)$

$i(t) \rightarrow$ Hilbert Transformation $\rightarrow \tilde{i}(t)$

$$H\{x(t)\} = x_{HT}(t) \quad ; \quad x_{HT}(t) = \frac{1}{\pi} \cdot \int_{-\infty}^{\infty} \frac{x(\tau)}{\tau - t} d\tau$$

$H\{x(t)\}$ properties: $\text{Mod}[H] = 1$, $\text{Arg}[H] = -\pi/2$

\rightarrow The Hilbert Transformer is a **90 degrees** phase-shifter!

From trigonometric properties, the following relationships can be derived:

$$\hat{I}(t) = \sqrt{i(t)^2 + \tilde{i}(t)^2}$$

Instantaneous current envelope

$$f_o(t) = \frac{1}{2 \cdot \pi} \cdot \frac{i(t) \cdot \frac{d}{dt} \tilde{i}(t) - \tilde{i}(t) \cdot \frac{d}{dt} i(t)}{\hat{I}(t)^2}$$

Instantaneous current frequency

$$M_{stZ}(t) = \frac{\sqrt{u(t)^2 + \tilde{u}(t)^2}}{\sqrt{i(t)^2 + \tilde{i}(t)^2}}$$

Short - Time
Magnitude of the
Load Impedance

$$\sin(\phi_u(t) - \phi_i(t)) = \frac{i(t) \cdot \tilde{u}(t) - \tilde{i}(t) \cdot u(t)}{\sqrt{i(t)^2 + \tilde{i}(t)^2} \cdot \sqrt{u(t)^2 + \tilde{u}(t)^2}}$$

Short - Time
Argument Sinus
of the Load
Impedance

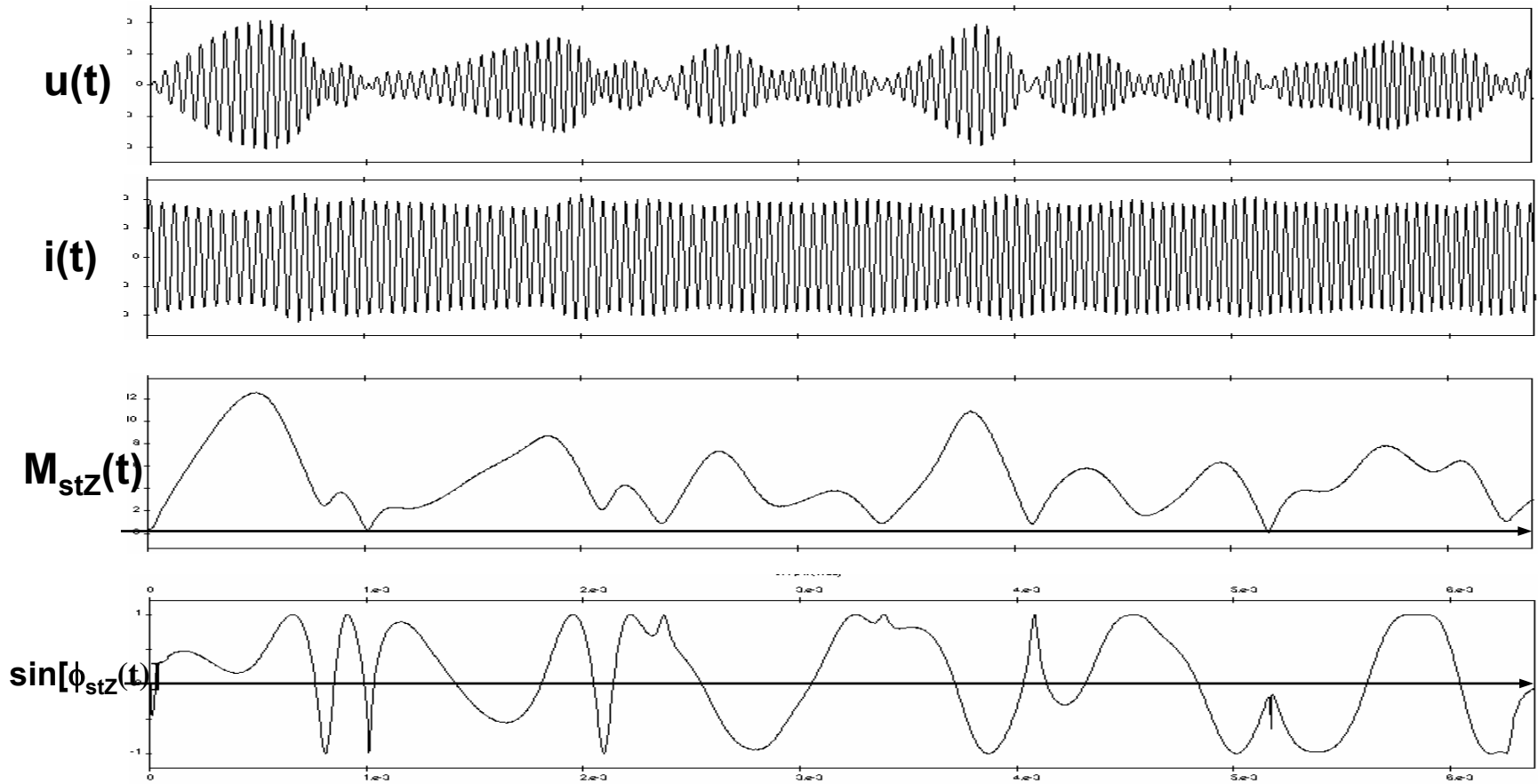
Let us define the **"Short-Time"** Active Power as follows:

$$P_{\text{active}}(t) = \frac{1}{2} \cdot \hat{U}(t) \cdot \hat{I}(t) \cdot \cos \left[\phi_{\text{stZ}}(t) \right]$$

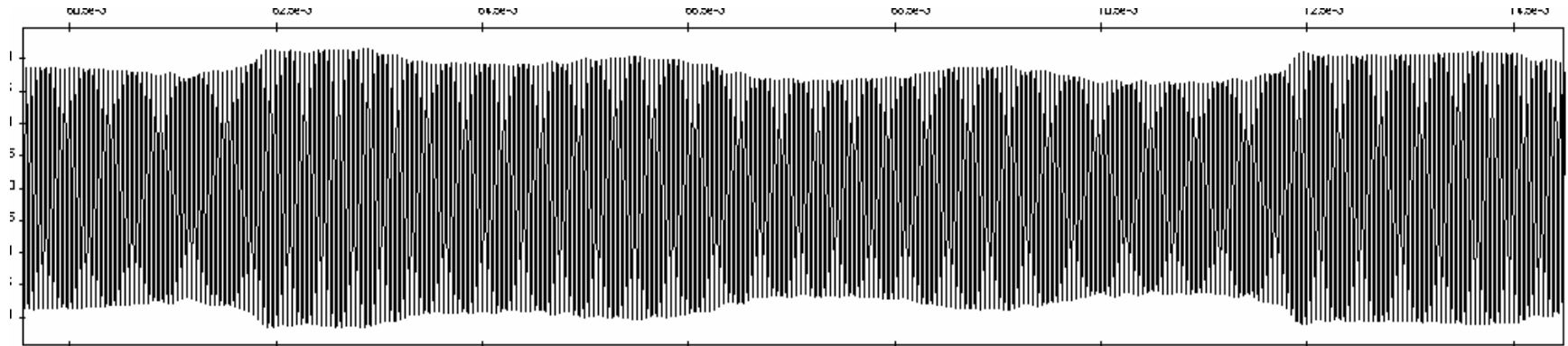
Then:

$$P_{\text{active}}(t) = \frac{i(t) \cdot u(t) + \tilde{i}(t) \cdot \tilde{u}(t)}{2}$$

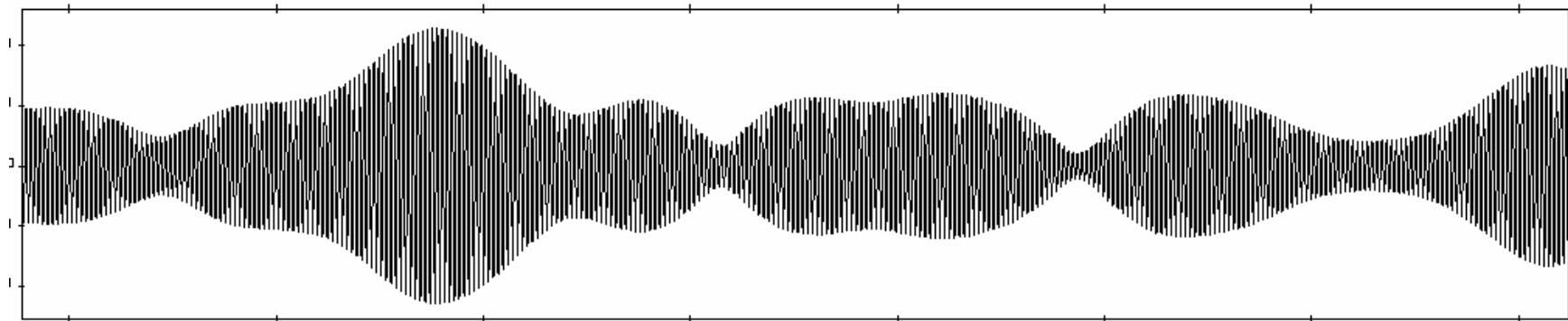
Computer Simulation Example



Field Test Measurements (from MMM ultrasonic system)

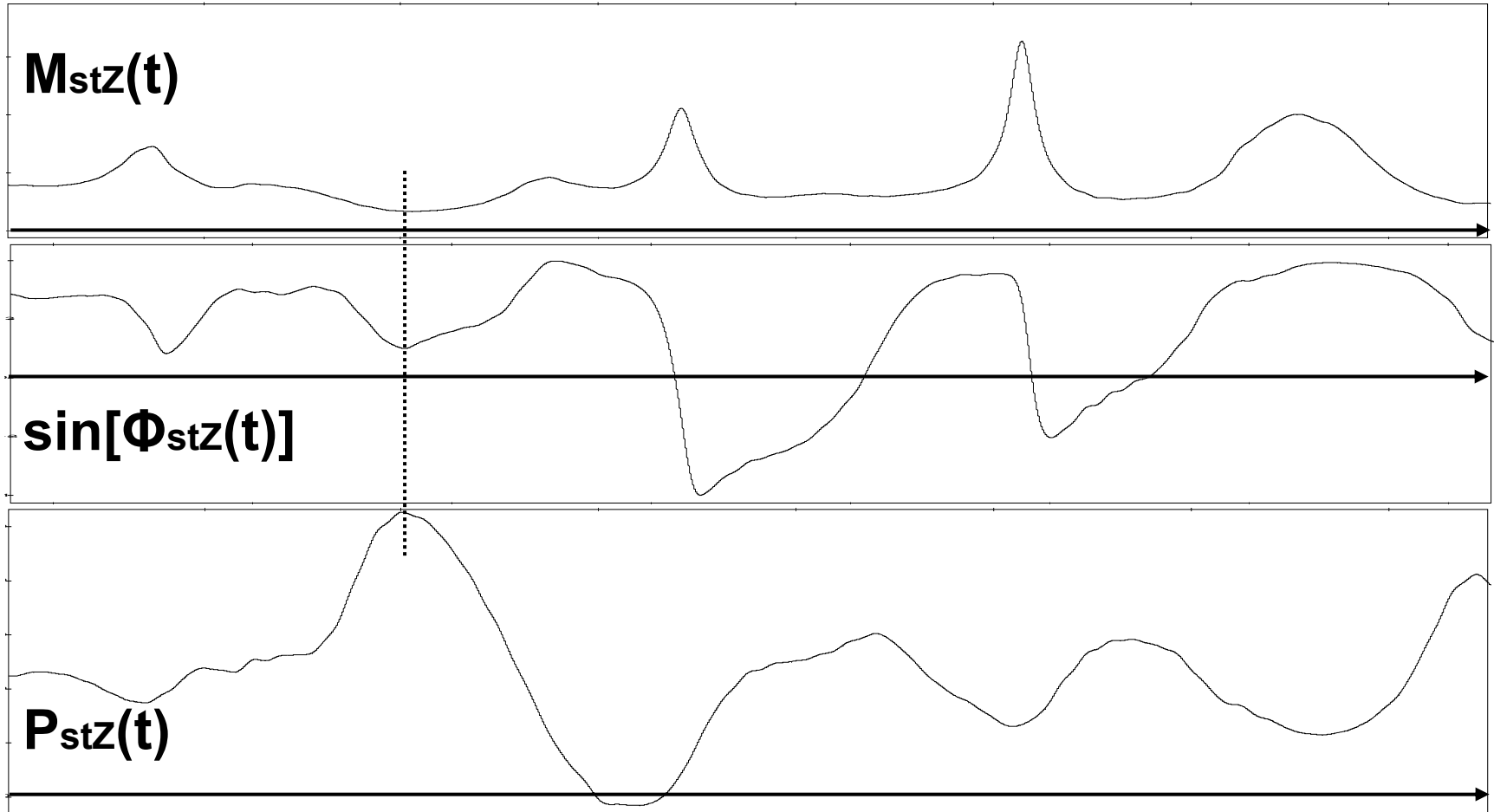


$u(t)$



$i(t)$

Computed "Short-Time" Magnitude, Argument, Active Power of the Load



Conclusion

*Many Processes with fast changing
load conditions can greatly benefit
from "real-time"*

load parameters estimations

*This can also dramatically enhance
the global performances of some
industrial processes.*