Abstract—Head flapping has often been considered to be deleterious for obtaining a tonpilz transducer with broadband, high power performance. In the present work, broadband, high power tonpilz transducers have been designed using the finite element (FE) method. Optimized vibrational modes including the flapping mode of the head are effectively used to achieve the broadband performance. The behavior of the transducer in its longitudinal piston mode and in its flapping mode is analyzed for in-air and in-water situations. For the 37.8% bandwidth of the center frequency from 28.5 to 41.8 KHz, the amplitude variation of the transmitting voltage response (TVR) does not exceed ±2 dB and a maximum TVR of 146.8 dB (ref. 1 μPa/volt at 1 meter) is obtained. Reasonable agreement between the experimental results and the numerical results is achieved. A maximum sound pressure level of 214.8 dB can be expected. Further numerical calculation indicates that there is potential for increasing the bandwidth by varying other parameters in the design.

I. INTRODUCTION

THE TONPIlz TRANsDUCER is one of the most popular types of sonar transducer, and its low cost, simplicity, and good performance are well known. The typical configuration of a tonpilz transducer is shown in Fig. 1. The conventional tonpilz transducer, as a longitudinal vibrator, has a limited bandwidth. Due to the imperative needs for high accuracy and high resolution sonar systems, broadband tonpilz transducers are required. The bandwidth of the tonpilz transducer may be improved to a limited extent by reducing the thickness or increasing the front diameter of the cone head. Both of these approaches may lead to the appearance of flexural resonances of the head. In the past, sophisticated numerical techniques (e.g., FE) were not available. As a consequence, the vibrational and the acoustical behavior of a tonpilz transducer with many modes of vibration, could not be well understood and optimized sufficiently. The presence of the flexural mode of the head, often referred to as head flapping, has been recognized for many years and has usually been considered to have a negative influence on the performance, in particular by reducing the bandwidth and acoustic power output [1]. The recommended design procedure to avoid problems is to ensure that the flapping resonance frequency is well above the operating frequency, which is normally the resonance frequency of the fundamental piston mode of the transducer [2]. The in-air vibration modes, including the flapping mode of the tonpilz transducer, have been investigated using the FE method by, for example, Hamonic [3] and Decarpigny et al. [4]. An alternative approach, using an equivalent circuit method [5], has been used by Butler et al. [6]. In contrast to the normal view that head flapping is undesirable, the investigation has shown that it is possible to use the flexural motion to a positive effect.

Various methods have been used to achieve broadband design. Two of the successful achievements are the matching layer technique [7]–[9] and the design of multimass tonpilz transducers [1], [10], respectively. The matching layer technique uses one or more layers on the front face of the radiating head, where the characteristic impedances of the different layers are optimized [11]. A transducer which has a −6 dB bandwidth of 55.2% has been reported [8]. The transducer comprises three layers of alumina-epoxy composites in different percentages. The multi-mass design seeks to transform the normal tonpilz configuration of spring (piezoceramic) and double-masses (head and tail) into one with three masses and two springs [1], [10]. The ceramic stack of the transducer is divided into two parts, constituting two springs, and an additional metal mass is assembled between the two ceramic springs. The three masses and two springs change the transducer into a two-resonance system leading to a camel-shaped transmitting voltage response (TVR) with a broadband performance. A −6 dB bandwidth of about 86% has been found for this type of design [1]. Most of the attempts at obtaining broadband tonpilz transducers, including the multilayered and the multimass approaches, lead to complications in manufacturing and assembling of the transducers.

In this paper, the possibilities of achieving a broadband tonpilz transducer using different vibrational modes, while maintaining the simple conventional configuration, is investigated. The basic modes used are the piston mode of the whole transducer and the flapping mode of the head, respectively. In-air analysis is performed to understand the free vibrational behavior at different modes. In-water analysis is mainly concentrated on obtaining the broadband TVR by optimizing the transducer structure. The phenomenon of in-air mode shape change between the flapping and longitudinal piston modes is found. The water-loaded vibrational displacements of the transducer and the pressure TVR provide comprehensive understanding of the behavior of the multimode broadband tonpilz transducer.
II. DESIGN DESCRIPTION

The multimode tonpilz transducer studied has the simple conventional configuration shown in Fig. 1. The cone radiation head is made of light aluminum alloy while the tail mass is made of brass. Two Navy type I (PZT4) piezoceramic rings are used for the active material. The steel bias bolt compresses the two piezoceramic rings and ensures that stresses in the ceramic stack are always compressive. In earlier designs, the cone head was designed to provide a larger radiating area, improved radiation impedance, and better impedance matching, and so lead to a relatively higher bandwidth and larger acoustic power. In the multimode broadband design, the head is the most critical part. The design procedures are as follows. First, the ordinary one-dimensional transmission line method can be used to obtain the primary geometrical dimensions of the transducer (e.g., the thickness of the tail and the head). Second, the in-air FE model analysis may be used to find the fundamental piston mode and the fundamental flapping mode, respectively. The angle of the taper of the cone is selected on the criterion that the resonance frequencies of the flapping and piston modes should be neither too close nor too separated. Third, the in-water analysis may be used to optimize the geometrical dimensions to some extent with the aim of increasing the bandwidth of the TVR. The design procedures are the same when other modes are used to extend the bandwidth (e.g., the mode related to the prestress bolt, where the variable parameter is the bolt diameter).

III. Finite Element Analysis

A commercial FE package (i.e., ANSYS) is implemented for the calculation. The transducer is modeled as a continuous structure. The electrode, which is 0.25 mm thick, is also modeled. Due to the large prestress, the glue layers are very thin compared to the wavelength at the working frequencies studied. Thus, the glue was not taken into account. 2-D axisymmetric triangle and quadrilateral elements are used jointly in the FE model. For in-water harmonic analysis, the fluid-structure interaction and farfield acoustic absorption capabilities of the FE code are exploited, respectively [12].
head. The dependencies of the resonance frequencies on the geometrical sizes is used for optimizing the resonance frequencies at different modes to obtain a wideband TVR. A tonpilz transducer having resonance frequencies of different modes that are too close may not exploit the bandwidth capability of the multimode transducer, while one that has very separated resonances could result in a serious reduction in the TVR at intermediate frequencies. In the multimode design, mode coupling between the longitudinal piston mode and the flapping mode produces somewhat complicated in-air and in-water mode shapes. The modes superimpose together and neither a pure piston mode nor a pure flapping mode exists in the frequency regime studied. A phenomenon, namely the change of in-air dominant mode shape, has been found. When the diameter of the front and the back surface of the head are not too different (e.g., 56 mm and 40 mm, respectively) the first mode is longitudinal piston dominant while the second mode is flapping dominant. When the diameter of the front face increases above a certain value, the property of the first mode changes from longitudinal piston dominated to flapping dominated. This can be demonstrated by the vector displacements on the front and the back of the transducer in Figs. 4 and 5. In Figs. 4(a) and 5(b), the opposite directions of the displacements at two ends in the central part of the transducer represent the $\lambda/2$ piston mode. In Figs. 4(b) and 5(a), the nodes in the central part of the transducer vibrate in the same direction forming in-phase body displacements, while the nodes in the edge part of the head vibrate in the opposite direction representing a typical flapping property of the head. The critical value of the diameter of the front surface of the head, at which the change of the dominant mode happens is about 64 mm in air.

B. In-water Analysis

In the FE analysis, the coupling between the transducer and water can be taken into account by implementing fluid-structure-interaction elements at the fluid-structure interface. By performing the in-water harmonic analysis, the in-water electrical impedance and TVR of the transducer can be predicted. The main purpose of optimizing the design is to obtain a broadband, low-ripple TVR of the transducer. The TVRs of the tonpilz transducers with different diameters of the front face of the head are calculated and shown in Fig. 6. The double resonance peaks form a camel-shaped TVR, allowing multimode broadband tonpilz transducers to be obtained.

The ripple in the bandwidth can be controlled by varying the diameter of the front face of the head. It may be noticed in Fig. 6 that the resonance frequency of the first mode drops more significantly than that of the second mode while the diameter increases. As shown in Fig. 6, the resonance frequencies of the first mode are 33.7, 31.0, and 27.7 KHz for the diameter of 56, 60, and 64 mm, respectively. By using an analytical method (i.e., equivalent circuit method), the resonance frequencies of fundamental piston mode are calculated to be 33.6, 32.2, and 30.9 KHz, accordingly. It can be proven, especially by the results from the equivalent circuit method, that the reduced resonance frequency of the first mode mainly results from the larger head mass and the water load mass of the head for increasing the head diameter. Due to the interaction between the transducer structure and the water medium, the vibrational behavior of the transducer becomes more complicated. The head flapping appears at much lower frequency than in air. It is more difficult to judge the vibrational characteristics by visualizing the deformed shapes. Therefore, another method is used to assess the vibrational behavior by calculating the surface displacements of the transducer. All displacements receive contributions from all the existing modes at a specified frequency. Typical points, or nodes, used for monitoring the modes are the central point and the edge point of the front surface of the head as well as the central point of the bolt on the
In-air analysis \( \text{Dh}=68 \text{ mm} \)

first mode: 28.57 kHz
flapping mode dominant

![Diagram](image)

Fig. 5. In-air surface displacements at the first two modes for a large value of the front diameter.

second mode: 39.2 kHz
longitudinal piston mode dominant

![Diagram](image)

back of the transducer, respectively. The displacements in the longitudinal direction as functions of frequency for a transducer with a front diameter of 60 mm are depicted in Fig. 7.

In the low-frequency region, \( f<30 \text{ KHz} \), \( V_a \) and \( V_b \) have the same directions representing the simple piston-type vibrational motion. As the frequency increases from 30.5 KHz, the flapping of the head appears and the mode shapes become complicated. The maximum negative value of \( V_b \) around 32 KHz indicates the significant influence of the flapping mode. Around 45 KHz, the maximum value of \( V_c \) indicates the bolt relevant mode. One may find by comparing the TVR in Fig. 6 and the displacements plots in Fig. 7 that the frequencies of the peaks in the TVR do not coincide with the frequencies at which \( V_a \) and \( V_b \) reach their peak amplitudes. This is due to the fact that the pressure field is formed by a combination of the various contributions from the surface of the transducer. Therefore, the properties of the integrated pressure could be different from the individual vibrational properties of the transducer structure.

The in-air longitudinal displacements around the resonance frequency of the first mode as a function of frequency are shown in Fig. 8. It can be seen from Fig. 8 that \( V_a \) and \( V_b \) have the same direction corresponding to the in-phase piston motion at the first mode. Note that in Fig. 7 \( V_a \) and \( V_b \) change to out-of-phase flapping motion while the transducer is water-loaded. Therefore, the head flapping appears at lower frequency than it appears in air due to the water load. Under these circumstances, the in-air modal analysis does not provide a reliable guide to its in-water vibrational behavior.

IV. Experimental Results

A tonpilz transducer prototype has been built on the basis of the optimized design aiming at high power broadband performance. The diameter of the head front is
Fig. 8. In-air longitudinal displacements of the three selected nodes of the transducer around the first mode.

Fig. 9. Measured and calculated transmitting voltage response.

Fig. 10. Measured and calculated impedance.

Fig. 11. Measured and calculated beam patterns at 30.4 KHz.

60 mm. The measured and calculated TVR results are shown in Fig. 9. The measured TVR value is somewhat lower than the numerical result in the frequency region between 25 and 43 KHz. Several possible factors (e.g., the mechanical losses and the difference between the real material data and the data used in the calculations) could result in the deviation. According to the measured TVR result shown in Fig. 9, for the 37.8% bandwidth of the center frequency from 28.5 to 41.8 KHz, the amplitude variation of the TVR does not exceed ±2 dB. According to the practical applied voltage limitation of 4000 volt/cm for Navy type I ceramics, the maximum sound pressure level is 214.8 dB (ref. 1 μPa at 1 meter). The calculated and measured in-water electrical resistance and reactance are plotted in Fig. 10. The measured and calculated beam patterns at 30.4 KHz are shown in Fig. 11.

It may be noticed in Figs. 9 and 10 that the third mode which is related to the piston mode of the prestress bolt does not appear in the measured TVR and impedance results. A possible explanation for this lies in the difficulty of modelling the screw joints at the head and tail of the bolt. The FE model is based on an assumption of an ideal connection, and this is not accurate enough to predict the results in the frequency regime in which the influence of the prestress bolt connection is significant. More research related to the influence of the screw joint is necessary.

V. FURTHER OPTIMIZATION

More calculations show that the bandwidth may be extended further using the vibrational mode of the optimized prestress bolt. Predicted TVRs of the tompilz transducer with different diameters of the bolt are shown in Fig. 12. It can be seen that the resonance frequency of the third peak in the TVRs decreases as the bolt diameter increases. However, the modal analysis shows that the in-air resonance frequency of the third mode does not have this dependency. The mechanism of this dependence between the third peak resonance frequency in TVR and the bolt di-
ameter is presently under investigation. At the same time, the amplitude in the trough of the TVRs increases leading to an improved bandwidth. For a prestress bolt with a diameter of 11.8 mm, the bandwidth is extended to 60% spanning the range 28 to 54 KHz, if the allowed TVR ripple is increased to 6 dB.

The assumption of an ideal connection of the bolt-head and bolt-tail joint connections in the FE model, instead of the actual screwed connection, could lead to a significant deviation between numerical results and experimental results near the bolt-dependent resonance frequencies. It could be helpful to minimize the deviation using a small-pitch screw combined with glued assembly.

VI. Conclusions

A broadband, high-power tonpilz transducer can be obtained using multimode operation including the flapping mode of the head. By using the fundamental longitudinal mode and the flapping mode together, the amplitude variation of the TVR does not exceed ±2 dB from 28.5 to 41.8 KHz. A maximum sound pressure level of 214.8 dB (ref. 1 μPa at 1 meter) can be expected according to the measured maximum TVR of 146.8 dB (ref. 1 μPa/volt at 1 meter). The vibrational mode in relation to the prestress bolt of the tonpilz transducer is another potential mode which can be used to improve the bandwidth further. In conjunction with the piston mode and the flapping mode, a -6 dB bandwidth of 60% is predicted.

The flapping mode of the cone head plays an important role in the multimode broadband design. For the transducer studied, the in-air modal analysis shows that the first mode shape is longitudinal piston dominant and the second is flapping dominant. But in water, the water load leads to the earlier appearance of the head flapping. This head flapping superposes to the piston mode leading to the deformed shape of flapping even at the resonance frequency of the piston mode. Due to the sensitive effect of the head mass and the load mass on the piston mode, the first resonance frequency in the TVR strongly depends on the front diameter of the head.

References


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